

Math 227
Spring 2021
Lecture 28



SG 36

Comparing at least 3 pop. means:

$$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$$

H_1 : at least one population mean is different **RTT**

CTS F \Rightarrow **STAT TESTS ANOVA(L1, L2, L3, ...)**
 P-value P

P-value $> \alpha \Rightarrow H_0$ valid, H_1 invalid

P-value $\leq \alpha \Rightarrow H_0$ invalid, H_1 valid

Given CTS F , **RTT**

Use **$F_{cdf}(CTS, E99, Ndf, Ddf)$**

$$Ndf = k - 1$$

k # of groups

$$Ddf = n - k$$

n Total Sample Size

Morning	ASternoon	Night
72 85	75 83	74 79
90 68	92 70	86 92
<u>100</u>	<u>98 75</u>	<u>100 65</u>
L1	L2	L3

Use $\alpha = .1$ to test the claim that All pop. means are equal.

$k=3$

$H_0: \mu_1 = \mu_2 = \mu_3$ Claim

$H_1: \text{at least one mean is different. RTT } n=5+6+6=17$

Morning \rightarrow L1
 ASternoon \rightarrow L2
 Night \rightarrow L3

STAT TESTS
 ANOVA(L1, L2, L3)

CTS $F = .007$
 P-value $P = .993$

NdS = $k-1 = 2$
 DdS = $n-k = 14$

P-value $> \alpha \Rightarrow H_0 \text{ valid} \Rightarrow \text{Valid claim}$
 $H_1 \text{ invalid}$

Support the claim
 FTR the claim

ANOVA \Rightarrow Analysis of Variance.

Given CTS $F = .007$ RTT NdS = 2
 DdS = 14

Find p-value.

$S_{cdS}(.007, F_{99}, 2, 14) = \boxed{.993}$

Students were randomly selected from 4 different schools. Here are their ages.

ELAC		Mt.SAC			Cal State LA			Cal Poly Pomona		
23	32	35	17	21	28	38	42	27	36	45
20	30	29	25	25	26	39	50	23	39	51
18	28		30			55			42	
<u>L1</u>		<u>L2</u>			<u>L3</u>			<u>L4</u>		

Use $\alpha = .01$ to test the claim that all pop. means are equal. $K=4$
 $n = 6+7+7+7 = 27$

$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$ claim

H_1 : At least one mean is different. RTT $Ndf = k-1 = 3$
 $Ddf = n-k = 23$

Clear all lists

ELAC \rightarrow L1

Mt.SAC \rightarrow L2

Cal State LA \rightarrow L3

Cal Poly Pomona \rightarrow L4

STAT

TESTS

ANOVA(L1, L2, L3, L4) [Enter]

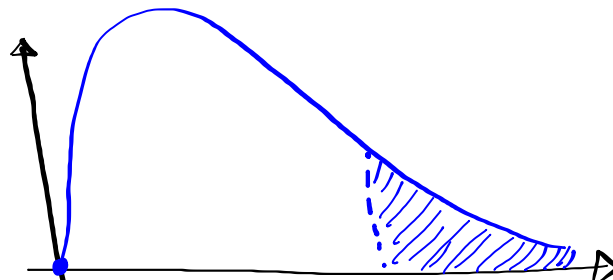
CTS F = 5.460

P-value P = .006

P-value $\leq \alpha \Rightarrow H_0$ invalid \Rightarrow invalid claim \Rightarrow Reject the claim
 $.006 \leq .01$ H_1 valid

Given CTS F = 5.460 RTT $Ndf = 3$
 $Ddf = 23$

Find P-value



$$Fcdf(5.460, E99, 3, 23) = .006$$

Same exam was given to 5-Different Colleges.
Here are the results for randomly selected exams:

From each school. $K=5$
 $n=5+5+4+5+5=24$

ELAC		Mt. SAC		Chaffey		PCC		Cetendale		
84	75	80	78	72	78	80	70	66	79	84
90	65	90	68	85	95	90	100	96	99	
<u>100</u> L5		<u>98</u> L4		<u>83</u> L3		<u>85</u> L2		<u>96</u> L1		

Test the claim that not all pop. means are equal.

$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5$ \rightarrow No $\alpha \rightarrow \alpha = 0.05$
 $ndf = k - 1 = 4$, $ddf = n - k = 19$

H_1 : At least one pop. mean is different. RTT, claim

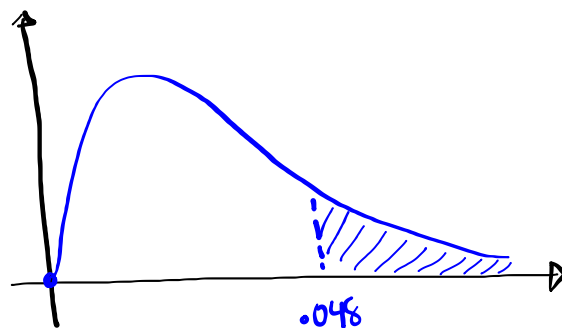
CTS $F = .048$	P-value $> \alpha$
P-value $P = .995$	

STAT
TESTS
ANOVA(L1, L2, L3, L4, L5)

H_0 valid $\hat{=}$ H_1 invalid
Invalid claim
Reject the claim

Given CTS $F = .048$
RTT
 $ndf = 4$
 $ddf = 19$

Find P-value



$f_{cdf}(.048, 4, 19) = .995$

P-value $> \alpha \Rightarrow H_0$ valid, H_1 invalid
P-value $\leq \alpha \Rightarrow H_0$ invalid, H_1 valid

SG 36
ANOVA